# TSD: A shape descriptor based on a distribution of tensor scale local orientation 

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#### Abstract

We present tensor scale descriptor (TSD) - a shape descriptor for content-based image retrieval, registration, and analysis. TSD exploits the notion of local structure thickness, orientation, and anisotropy as represented by the largest ellipse centered at each image pixel and within the same homogeneous region. The proposed method uses the normalized histogram of the local orientation (the angle of the ellipse) at regions of high anisotropy and thickness within a certain interval. It is shown that TSD is invariant to rotation and to some reasonable level of scale changes. Experimental results with a fish database are presented to illustrate and validate the method.


## 1 Introduction

Recent advances in the image acquisition technologies have increased the demand for effective image searching and browsing tools. Such tools should be able, for example, to retrieve images from large collections, which are similar to a query image. The images contain objects and the standard formats to represent the shape of these objects may be used for this purpose, as shape descriptors. In the MPEG-7 project, for instance, several principles have been adopted to measure the quality of a descriptor, such as its retrieval accuracy, robustness, compactness, general application, computational complexity, and hierarchical representation from coarse to fine [17]. In order to accomplish these goals, a descriptor should be simple, compact, insensitive to noise, affine-invariant, and at same time contain all relevant information to distinguish different images.

In this work, we present a shape descriptor based on the tensor scale concept $[26,27,29]$ - a morphometric parameter yielding a unified representation of local structure thickness, orientation, and anisotropy. That is, at any image point, its tensor scale is represented by the largest ellipse
(2D), or ellipsoid (3D), centered at that point and within the same homogeneous region.

The algorithmic framework to compute tensor scale, as originally proposed [26,27,29], is computationally expensive. To address this problem, we propose a simpler and yet effective implementation of the original method. Tensor scale has been demonstrated for image filtering, segmentation, and registration [26, 27,29]. In this paper, we discuss its applicability to create effective shape descriptors for content-based image retrieval.

The key idea is to represent each image by its normalized histogram of the local orientation (the angle of the ellipse) at regions of high anisotropy and thickness within a certain interval. The matching of two images involves correlation, registration, and absolute difference of area between their histograms to produce a similarity measure. This process is invariant to rotation and to some reasonable level of scaling, which does not affect the computation of the ellipses. The rotation angle may be easily found during the matching phase and could be used for image registration as well.

After giving the previous relevant study in Section 2, Section 3 presents our implementation of tensor scale. In Section 4, we present the tensor scale descriptor and its validation is done in Section 5. Section 6 states conclusion and discusses future work.

## 2 Background

Scale is a very used concept in image processing. Basically, scale-based approaches have been used in different applications (such as, image classification and retrieval) to represent and process images at various resolutions. Current researches in this area have focused on the promising notion of localized scale, which is space-variant resolution method.

Punam et al. have introduced a new local scale method called tensor scale $[26,27,29]$. Their approach is a natural evolution of their previous work based on a spherical
model $[26,28,30]$ to a richer model based on ellipses. The elliptical model overcome the major limitation of the spherical model, which is the lack of local structure orientation and anisotropy information.

The tensor scale at an image point is a parametric representation of the largest ellipse (ellipsoid in 3D) centered at that point and within the same homogeneous region, according to some predefined criterion. It yields a unified representation of local structure thickness, orientation, and anisotropy, serving as a unique tool to analyze architecture of image structures without explicit segmentation [26,27, 29]. For a given pixel, the largest ellipse within the same homogeneous region is determined by tracing sample lines from 0 to 180 degrees around that pixel and computing the following steps:

1. Intensity computation along each sample line.
2. Location of two optimum edge points on each sample line.
3. Repositioning of the edge locations to points equidistant to the given pixel, following the axial symmetry of an ellipse.
4. Computation of the best-fit ellipse to the repositioned edge locations.

These steps are performed for each image pixel until all ellipses have been computed. Next, we briefly explain these steps as originally proposed in $[26,27,29]$.

For a given sample line passing through a given pixel, the method considers the two radially opposite segments from that point (center of the pixel) in order to locate the closest edge points, being one on each segment. The distribution of the sample lines is approximately uniform over the entire angular space (from 0 to 180 degrees) around the pixel. This is important to guarantee invariance to rotation. A unit vector is used to represent the direction of each segment. There are $m$ pairs of these mutually opposite unit vectors, denoted by $\left(\vec{\tau}_{1}, \vec{\tau}_{1}^{\prime}\right),\left(\vec{\tau}_{2}, \vec{\tau}_{2}^{\prime}\right), \ldots,\left(\vec{\tau}_{m}, \vec{\tau}_{m}^{\prime}\right)$. The segment with direction $\vec{\tau}_{i}$ emanating from a pixel $p$ is denoted by $\pi_{i}^{(p)}:[0, L] \rightarrow \Re^{2}$ and its opposite segment with direction $\vec{\tau}_{i}^{\prime}$ is denoted by $\pi_{i}^{\prime(p)}$.

$$
\begin{equation*}
\pi_{i}^{(p)}(\lambda)=p+\lambda \vec{\tau}_{i} \quad \mid \quad \lambda \in[0, L] \tag{1}
\end{equation*}
$$

These segments have maximum length $\lambda=L$ (an input parameter that represents the largest local scale). Previous experiments have shown that suitable values of $L$ are from 8 to 15 points. Larger values increase the computational cost, usually without a proportional gain in scale estimation. An intensity profile $f_{i}^{(p)}(\lambda)$ on each segment is computed by interpolating image intensities.

The local edge detection on each segment is based on the maximum $\mu_{\pi_{i}^{(p)}}^{U P}$ and minimum $\mu_{\pi_{i}^{(p)}}^{D N}$ intensity profiles along the segment.

$$
\begin{align*}
\mu_{\pi_{i}^{(p)}}^{U P}(\lambda) & =\max _{x=1,2, \ldots, \lambda} f_{i}^{(p)}(x),  \tag{2}\\
\mu_{\pi_{i}^{(p)}}^{D N}(\lambda) & =\min _{x=1,2, \ldots, \lambda} f_{i}^{(p)}(x) \tag{3}
\end{align*}
$$

The main goal here is to handle the cases of "step-up" and "step-down" edges separately, filtering locally disconnected structures of similar intensities [26,27,29]. A conventional edge detector is subsequently applied to locate an edge point on the minimum and maximum intensity profiles. The optimum edge location on the segment is then determined as the one closer to the point $p$.

Optimum edge location is an active research area $[5,11$, 21,32 ]. Punam et al. have adopted the $L o G$ function proposed by Marr and Hildreth [21] to compute the optimum edge location on the $\mu_{\pi_{i}^{(p)}}^{U P}$ and $\mu_{\pi_{i}^{(p)}}^{D N}$ profiles. The edge location is given as the first (from the pixel $p$ ) zero-crossing point of the $L o G$ function, where the intensity gradient is above a threshold. The intensity gradient is computed by convolving the minimum and maximum profiles with the first derivative of a Gaussian.

The computed edge locations along all sample lines are used to fit an ellipse centered at the point $p$. Since two radially opposite points on a given line are expected to be equidistant to $p$, they need to be repositioned. The method selects the edge point closer to $p$ on each pair of opposite segments and replaces the other by the reflection of the selected point.

The computation of the best-fit ellipse is accomplished in two sub-steps.

## 1. Determination of ellipse orientation.

## 2. Computation of the lengths of the semi-axes.

Punam et al. used principal component analysis [13] to implement the first sub-step. In their solution, the orientation $\theta$ of an ellipse is given by the smaller angle between the eigen-vector associated with the largest eigen-value of the covariance matrix $\Sigma$ and the horizontal axis, where the elements $\Sigma_{i, j}$ of $\Sigma$ are defined as follows:

$$
\begin{align*}
\Sigma_{1,1} & =\frac{1}{2 m} \sum_{i=1,2, \ldots, 2 m}\left(x_{i}-x_{p}\right)^{2}  \tag{4}\\
\Sigma_{2,2} & =\frac{1}{2 m} \sum_{i=1,2, \ldots, 2 m}\left(y_{i}-y_{p}\right)^{2}  \tag{5}\\
\Sigma_{1,2} & =\frac{1}{2 m} \sum_{i=1,2, \ldots, 2 m}\left(x_{i}-x_{p}\right)\left(y_{i}-y_{p}\right)  \tag{6}\\
\Sigma_{2,1} & =\Sigma_{1,2} \tag{7}
\end{align*}
$$

The points $\left(x_{i}, y_{i}\right) \mid i=1,2, \ldots, 2 m$ are the edge points after the reposition phase and $\left(x_{p}, y_{p}\right)$ are the coordinates of pixel $p$ (the central point of the ellipse).

The second sub-step is accomplished by minimizing the error function below, where $a$ and $b$ are the lengths of the two semi-axes.

$$
\begin{equation*}
f_{\text {error }}=\sum_{i=1,2, \ldots, 2 m}\left[1-\frac{u_{i}^{2}}{a^{2}}-\frac{v_{i}^{2}}{b^{2}}\right]^{2} \tag{8}
\end{equation*}
$$

where $\left(u_{i}, v_{i}\right) \mid i=1, \ldots, 2 m$ are the relative coordinates of the repositioned edge points with respect to $p$ and after rotation by angle $-\theta$, such that the ellipse's major semi-axis becomes aligned to the horizontal axis. To minimize the error function, the partial derivatives of $f_{\text {error }}$ with respect to $a$ and $b$ must be zero. It may be proved that $a$ and $b$, which minimize $f_{\text {error }}$, are

$$
\begin{align*}
a & =\sqrt{\frac{C \cdot C-D \cdot E}{C \cdot B-A \cdot E}}  \tag{9}\\
b & =\sqrt{\frac{C \cdot C-D \cdot E}{A \cdot C-D \cdot B}} \tag{10}
\end{align*}
$$

where $A, B, C, D$ and $E$ correspond to

$$
\begin{align*}
A & =\sum_{i=1,2, \ldots, 2 m} u_{i}^{2},  \tag{11}\\
B & =\sum_{i=1,2, \ldots, 2 m} v_{i}^{2}  \tag{12}\\
C & =\sum_{i=1,2, \ldots, 2 m} u_{i}^{2} v_{i}^{2}  \tag{13}\\
D & =\sum_{i=1,2, \ldots, 2 m} u_{i}^{4}  \tag{14}\\
E & =\sum_{i=1,2, \ldots, 2 m} v_{i}^{4} \tag{15}
\end{align*}
$$

In the following, $\vec{l}_{1}(p)$ and $\vec{l}_{2}(p)$ denote the two semiaxes of the ellipse centered at pixel $p$, where $\left\|\vec{l}_{1}(p)\right\| \geq$ $\left\|\vec{l}_{2}(p)\right\|$. The ellipse just computed gives us three factors - orientation $\theta$ of the major semi-axis $\vec{l}_{1}(p)$, anisotropy $\left(\sqrt{1-\left\|\vec{l}_{2}(p)\right\|^{2} /\left\|\vec{l}_{1}(p)\right\|^{2}}\right)$, and thickness $\left(\left\|\vec{l}_{2}(p)\right\|\right)$. For display purpose, these attributes are represented as a 2D image using the HSI color coding. It is adopted hue (H) for orientation, saturation (S) for anisotropy, and intensity (I) for normalized thickness. One may also use the square root of the normalized thickness to achieve better visualization at low thickness values.

## 3 Faster tensor scale computation

The main problem of tensor scale, as originally proposed [26,27,29], is its expensive computational time. Its
extension to 3 D is almost prohibitive. It is not difficult to verify that tensor scale would take hours to be computed for typical 3D image datasets running on conventional PCs. The implementation we propose next is simpler and yet effective. Instead of using the previous complex edge detection scheme, we adopted another criterion to define the homogeneous region around a given pixel, which leads to faster implementations. Our approach does not need the reposition phase and we have also improved the ellipse computation phase.

During the edge location phase, our approach is to go along each pair of opposite segments, alternately and at same time, instead of going along one entire segment by turn. When the edge location is found on a segment, the opposite edge point is already in the correct position, and therefore, reposition phase is no longer necessary. This is a great improvement because, when there are one edge point far away of $p$ on one segment and another edge point close to $p$ on the opposite segment, these segments could be traversed in a naive order according to the previous execution way. In our implementation, the shortest execution way is always guaranteed.

The original approach for edge detection also involves the standard deviation (a scale parameter) of the Gaussian and $L o G$ functions, and a threshold on the intensity gradient. Unfortunately, there exists no natural scale or gradient threshold which can be defined a priori to distinguish edges from non-edges. Edge detectors are typically designed to recover abrupt discontinuities in an image, however the edges of physical structures are usually blurred. Although larger scales are more suitable to detect smooth intensity transitions, while smaller scales may detect fine details [11], we will always run the risk of missing true edges. Besides, the use of the filtered intensity profiles $\mu_{\pi_{i}^{(p)}}^{U P}$ and $\mu_{\pi_{i}^{(p)}}^{D N}$ has a serious drawback. It duplicates the efforts in edge detection and forces us to compute the gradient on-the-fly for each segment.

In view of the difficulties above, we noted that what is really needed is a simple method that correctly detects edges, when they are abrupt discontinuities, and stops the edge detection process on smooth transitions to a different region. The key idea is that we are not interested in the exact location of complex edges. It is better to miss the right position of an edge by one or two pixels than lose it at all, as often happens when using a threshold on the intensity gradient.

We use two connected thresholds, th1 and th2 (i.e., $t h 2=n \cdot t h 1$, where $n \in[2,4]$ ), where the first is the maximum expected absolute intensity difference within homogeneous regions of the image and the second is the maximum cumulative absolute intensity difference allowed inside a homogeneous region. Both thresholds are computed with respect to the intensity of the central pixel $p$. The first tries
to capture abrupt discontinuities, while the second aims at stopping the edge detection process in the case of smooth intensity transitions. Each two opposite segments are traversed alternately at the same time. The absolute intensity difference $d$ between the current point and $p$ is computed and compared to $t h 1$. If $d \leq t h 1$, then it is cumulated into a variable $c$, whose value is compared to $t h 2$. The process stops either when $d>t h 1$ (abrupt transition) or when $c>t h 2$ (smooth transition).

In the case of binary images, the edge detection phase is trivial. We just stop traversing a pair of opposite segments, when one of them reaches the background. The rest of the algorithm is the same.

To improve the ellipse computation phase, we use a more straightforward solution. Instead of using the principal component analysis [13] to compute the ellipse's orientation $\theta$ (which involves determining the eigen-values and eigen-vectors), we define a function $g(\gamma)$ that gives us the angle $\theta$ directly.

$$
\begin{align*}
g(\gamma) & =\sum_{i=1,2, \ldots, 2 m}\left[x_{i}^{\prime \prime 2}-y_{i}^{\prime \prime}\right], \quad \text { where }  \tag{16}\\
x_{i}^{\prime \prime} & =x_{i}^{\prime} \cos \gamma-y_{i}^{\prime} \sin \gamma  \tag{17}\\
y_{i}^{\prime \prime} & =x_{i}^{\prime} \sin \gamma+y_{i}^{\prime} \cos \gamma \tag{18}
\end{align*}
$$

$\left(x_{i}^{\prime}, y_{i}^{\prime}\right)$ are the relative coordinates of the edge points with respect to the center $p=\left(x_{p}, y_{p}\right)$ of the ellipse, and $\left(x_{i}^{\prime \prime}, y_{i}^{\prime \prime}\right)$ are the new coordinates after applying a rotation by angle $\gamma$ (i.e., $\gamma$ is a candidate for $-\theta$ ). The ellipse's orientation is obtained from the value of $\gamma$ which maximizes the function $g$.

By setting the derivative of this function to zero $\left(g^{\prime}(\gamma)=\right.$ 0 ), it can be shown that $\gamma$ has the form.

$$
\begin{align*}
\gamma & =\frac{\arctan \left[\frac{2 \cdot F}{G-H}\right]}{2}, \text { where }  \tag{19}\\
F & =\sum_{i=1,2, \ldots, 2 m} x_{i}^{\prime} \cdot y_{i}^{\prime}  \tag{20}\\
G & =\sum_{i=1,2, \ldots, 2 m} y_{i}^{\prime 2}  \tag{21}\\
H & =\sum_{i=1,2, \ldots, 2 m} x_{i}^{\prime 2} \tag{22}
\end{align*}
$$

We have to observe that $g^{\prime}(\gamma)=0$ may also imply that $g$ is minimum and the difference between the maximum and the minimum values is $\pi / 2$. This situation can be corrected as follows.

$$
\begin{array}{ll}
\operatorname{if}(F<0.0 \quad \text { and } \quad \gamma<0.0) & \gamma \leftarrow \gamma+\pi / 2  \tag{23}\\
\text { else if }(F>0.0 \quad \text { and } \quad \gamma>0.0) & \gamma \leftarrow \gamma-\pi / 2
\end{array}
$$

The above approach is very simple and yet effective. One may also note that due to the symmetry of the ellipse, it is
not necessary to perform sums $F, G$, and $H$ for all edge points. We may only consider one point for each pair of opposite segments, since $y_{i}^{\prime 2}=\left(-y_{i}^{\prime}\right)^{2}, x_{i}^{\prime 2}=\left(-x_{i}^{\prime}\right)^{2}$, and $x_{i}^{\prime} \cdot y_{i}^{\prime}=\left(-x_{i}^{\prime}\right) \cdot\left(-y_{i}^{\prime}\right)$. Thus, the sums $F, G$, and $H$ will be half sized. The same observation also applies to the computation of the length of the semi-axes. More specifically, for each opposite pair of segments we may add only once any of the two opposite edge points during $A, B$, $C, D$, and $E$ computations.

## 4 Content-based image retrieval using tensor scale

Distinct objects often present different tensor scale local orientation distributions of their shape, or even of their texture. The tensor scale descriptor (TSD) is based on this statement. We first compute the tensor scale parameters for the original image and then analyze the local orientation histogram. The computation of the local orientation histogram only considers pixels of high anisotropy and with thickness within a certain interval. This is done because pixels with either low anisotropy or high thickness do not have a well defined orientation and because pixels with low thickness stand over the edges and have their orientation influenced by pixel geometry.

The local orientation histogram is circular. The effect of image rotation on it is just the displacement by a constant offset. The matching of two given images is made by taking the absolute difference of area between their histograms, after correcting the displacement between them by correlation. The maximum correlation between two histograms gives us the best offset. Therefore, the process is invariant to rotation. To make the method more insensitive to scale, we use normalized histograms.

Figure 1a shows a fly wing image. The tensor scale image of Figure 1a and of its rotation by $15^{\circ}$ are shown in Figure 1b, together with the circle on the right which represents the HSI color coding. As we may see, the two tensor scale images have a very good agreement. Figure 1c illustrates the matching of their local orientation histograms, after offset correction by correlation. Note that we can find the rotation angle by converting the offset to degrees and this information could be used for registration.

## 5 Experimental Results

This section compares the tensor scale descriptor (TSD) to commonly used shape descriptors.

### 5.1 Shape database

The shape database is a set with one thousand and one hundred fish contours obtained from [31]. Since there is


Figure 1. (a) A fly wing image. (b) The tensor scale images of (a) and of its rotation by $15^{\circ}$, and a circle representing the HSI color coding. (c) The matching of their local orientation histograms by correlation.
no semantic definition of classes for the fish contours in this database, we defined a class as consisting of 10 different manifestations of each contour by rotation and scaling. Then, the problem consists of 1100 classes with 10 shapes each.

### 5.2 Evaluated descriptors

Table 1 shows the set of implemented shape descriptors. Beam Angle Statistics and Curvature Scale Space have been widely used as shape descriptors [1-3,24]. Many versions

| Descriptor Id | Descriptor Name |
| :---: | :---: |
| TSD | Tensor Scale Descriptor |
| CCS | Convex Contour Saliences |
| CSS | Curvature Scale Space |
| BAS | Beam Angle Statistics |

Table 1. List of evaluated descriptors.
of these methods have been proposed, but, in this work, we consider conventional implementations.

Convex Contour Saliences (CCS): The CCS of a contour is definined as the influence areas of its higher curvature convex points [7, 8]. Previous work [7] has shown that CCS outperformes Multiscale Fractal Dimension [7], Fourier Descriptors [12, 22], Moment Invariants [10, 14], CSS [1,24] and BAS [3] with respect to the multiscale separability measure [7]. Experiments with Precision $\times$ Recall have also shown better results with the CCS as compared to CSS, Fourier Descriptors, and Moment Invariants [8].

Curvature Scale Space (CSS): The CSS descriptor extraction algorithm is described in [1,24]. The CSS descriptor vector represents a multiscale organization of the curvature zero-crossing points of a planar curve. In this sense, the descriptor dimension varies for different shapes, thus a special matching algorithm is necessary to compare two CSS descriptors [24]. We implemented a C version of the Matlab prototype presented in [23].

Beam Angle Statistics (BAS): The BAS descriptor has been compared with several others [4, 6, 16, 19, 20, 24], including the CSS descriptor. In [3], it was shown that the BAS functions with 40 and 60 samples outperform all of them. The experiments of the present paper use the BAS descriptor with 60 samples. Basically, the BAS descriptor is based on the beams originated from a contour pixel. A beam is defined as the set of lines connecting a contour pixel to the rest of the pixels along the contour. At each contour pixel, the angle between a pair of lines is calculated, and the shape descriptor is defined by using the third-order statistics of all the beam angles in a set of neighborhoods. The similarity between two BAS moment functions is measured by an optimal correspondent subsequence (OCS) algorithm, as shown in [3].

### 5.3 Effectiveness measures

Our experiments rely on the creation of a shape-based image retrieval system, which can be characterized as follows. Assume that we have a database containing a large number of images. Given a user-defined query pattern (e.g., a query image), the system must rank the images stored in the image database in increasing order of their distance of the query image (similarity), according to the image content (i.e., the objects are represented by shape properties).

The purpose of our experiments is to evaluate the effectiveness of the similarity-search of different descriptors in retrieving relevant images. Effectiveness evaluation is a very complex task, involving questions related to the definition of a collection of images, a set of query images, a set of relevant images for each query image, and suitable retrieval effectiveness measures. In our case, we use each original image as query image and we consider its manifestations as relevant images.

In our experiments, we use two graphical measures: Precision vs. Recall and $\theta$ vs. Recall. Precision vs. Recall $(P \times R)$ curves are the commonest evaluation measure used in CBIR domain. Precision is defined as the fraction of retrieved images which is relevant to a query. In contrast, recall measures the fraction of the relevant images which has been retrieved. A recall is a non-decreasing function of rank, while precision can be regarded as a function of recall rather than rank.

A $\theta \times R$ curve can be seen as a variation of the $P \times R$. We define $\theta$ as the average of the precision values measured whenever a relevant image is retrieved. For $100 \%$ of recall, the $\theta$ value is equivalent to the average precision. The main difference between the measures is that, unlike precision, $\theta$ value is cumulative (i.e., its computation considers not only the precision at a specific recall but also the precision at previous recall levels).

In general, both curves $(P \times R$ and $\theta \times R)$ closest to the top of the chart indicates the best performance.

### 5.4 Experimental results

This section discusses our experimental results related to the effectiveness of the proposed Tensor Scale approach. We compare $T S D$ and the CBIR approaches reviewed in Section 5.2, showing that $T S D$ outperforms them. Figures 2 and 3 show respectively the $P \times R$ and $\theta \times R$ curves obtained for all descriptors.

Observe that the $T S D$ presents the best $P \times R$ curve (Figure 2). For the $\theta \times R$ curve (Figure 3), a similar result can be verified. Again, the $T S D$ outperforms the others.

Figure 4 shows examples of similarity retrieval using four different query images (first column) and by taking into account the TSD. Each returned image is accompanied with the distance value with respect to the query image. As we can see, TSD was able to return similar images in the first positions.

## 6 Conclusions and Future Work

We have presented a simpler and yet effective implementation of the tensor scale concept and proposed a tensor scale descriptor based on local orientation. The TSD


Figure 2. Precision versus Recall curve.


Figure 3. $\theta$ versus Recall curve.
was evaluated using a fish database (binary images) in order to compare its effectiveness for content-based image retrival with the ones obtained by other well known shape descriptors: Convex Contour Saliences [7, 8], Curvature Scale Space [1,24], and Beam Angle Stastistics [3]. The effectiveness of the proposed descriptors is evident regarding the Precision vs. Recall and $\theta$ vs. Recall curves. The presence of manifestations, obtained by rotating and scaling operations, in the relevant sets suggests that the TSD is more robust to these kind of transformations than the others.

We are currently creating an image database of fly wings to support research in Biology. Preliminary tests have shown that TSD on texture is very promising for fast identification of similar species of flies using content-based image retrieval. We also intend to investigate other simple ways of defining local orientation, such as the gradient field over the image [ $9,15,18,25,33$ ], and compare them with the TSD.
Query Image

Figure 4. Results of similarity retrieval for four query images (first column), using the TSD.

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